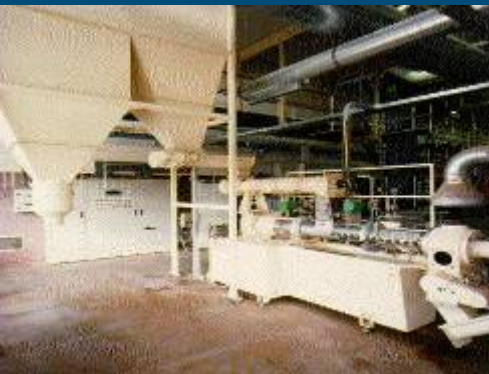


Modelling biochemical rumen functions with special emphasis on methanogenesis



Dr Jan Dijkstra
Animal Nutrition Group
Wageningen University



Overview

- Principles of mathematical modelling
- Empirical models of methane production
- Mechanistic models of methane production



Prediction ~ mathematical models

- Prediction requires use of models
- A model is an equation or set of equations that represent the behaviour of a system

France and Thornley (1984)

- A model can be viewed as an idea, hypothesis or relation expressed in mathematics
- Symbiosis between experimentation and modelling



Model classification

dynamic OR static

deterministic OR stochastic

mechanistic OR empirical

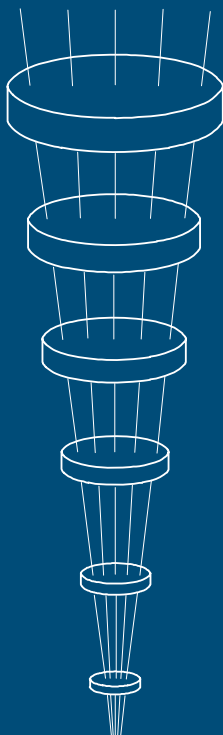
To put categories into a more familiar context, a model based on:

- regression analysis → static, stochastic, empirical
- linear programming → static, deterministic, empirical
- differential eqns → dynamic, deterministic,

mechanistic



Levels of organization

Level		Description of level
•		•
$i + 1$		Herd / flock
i		Animal
$i - 1$		Organ / tissue
$i - 2$		Cell
•		•

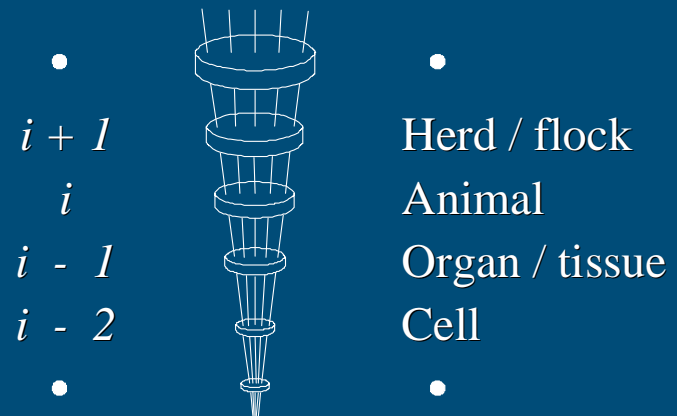
Dijkstra & France
(2005)



Properties of hierarchical systems

- Each level has its own concepts and language
- Each level is an integration of items from lower levels
- Successful operation of a level requires lower levels to function properly, but not necessarily vice versa

Level Description of level



Contributions of modelling

- Models provide a convenient data summary, useful for interpolation and cautious extrapolation
- Models make best use of (precious) data
- Models provide quantitative description and understanding of biological problems
- Modelling provides strategic and tactical support to research programmes
- Modelling allows exploration of possible outcomes when data are not available



Overview

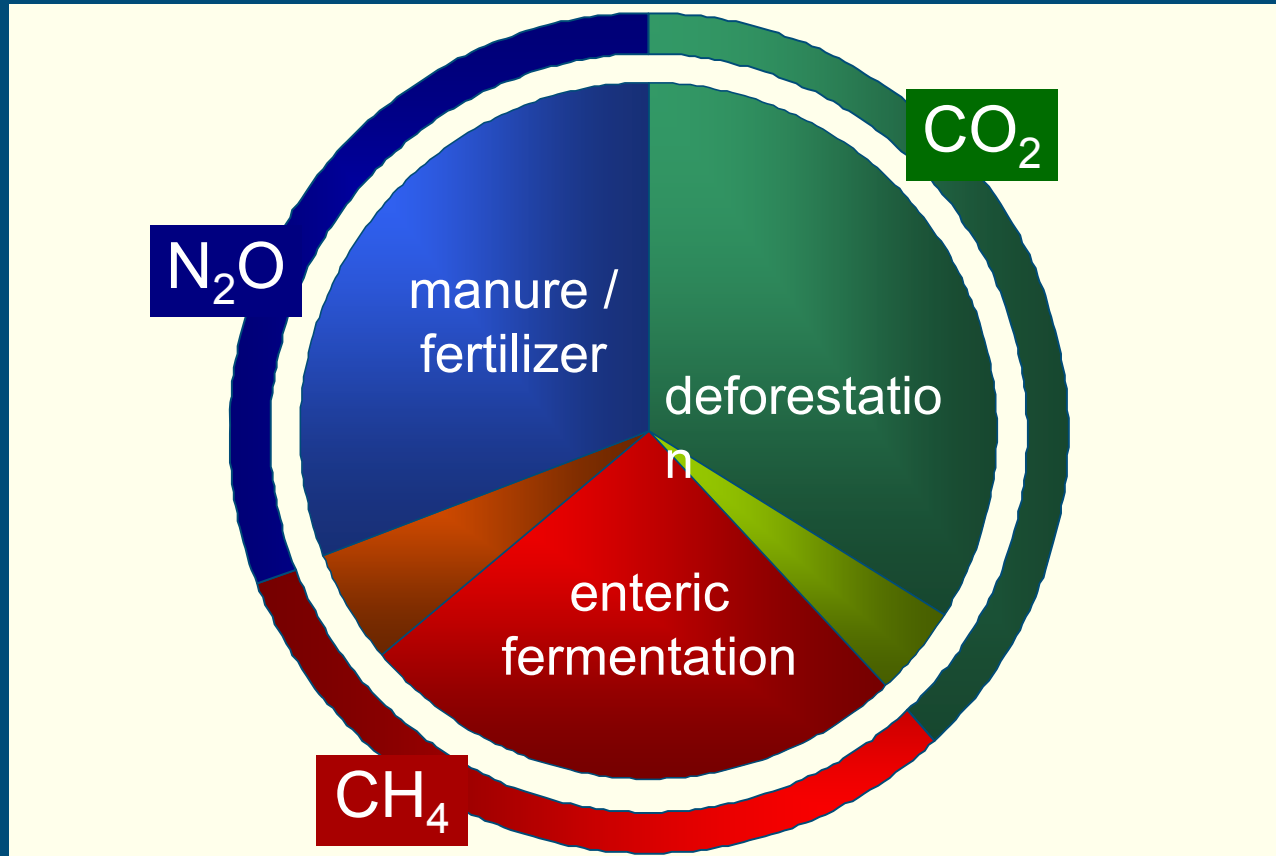
- Principles of mathematical modelling
- Empirical models of methane production
- Mechanistic models of methane production





Livestock greenhouse gases

FAO (2006)



GWP* -100 yr:

CO₂ 1

CH₄ 25

N₂O 298

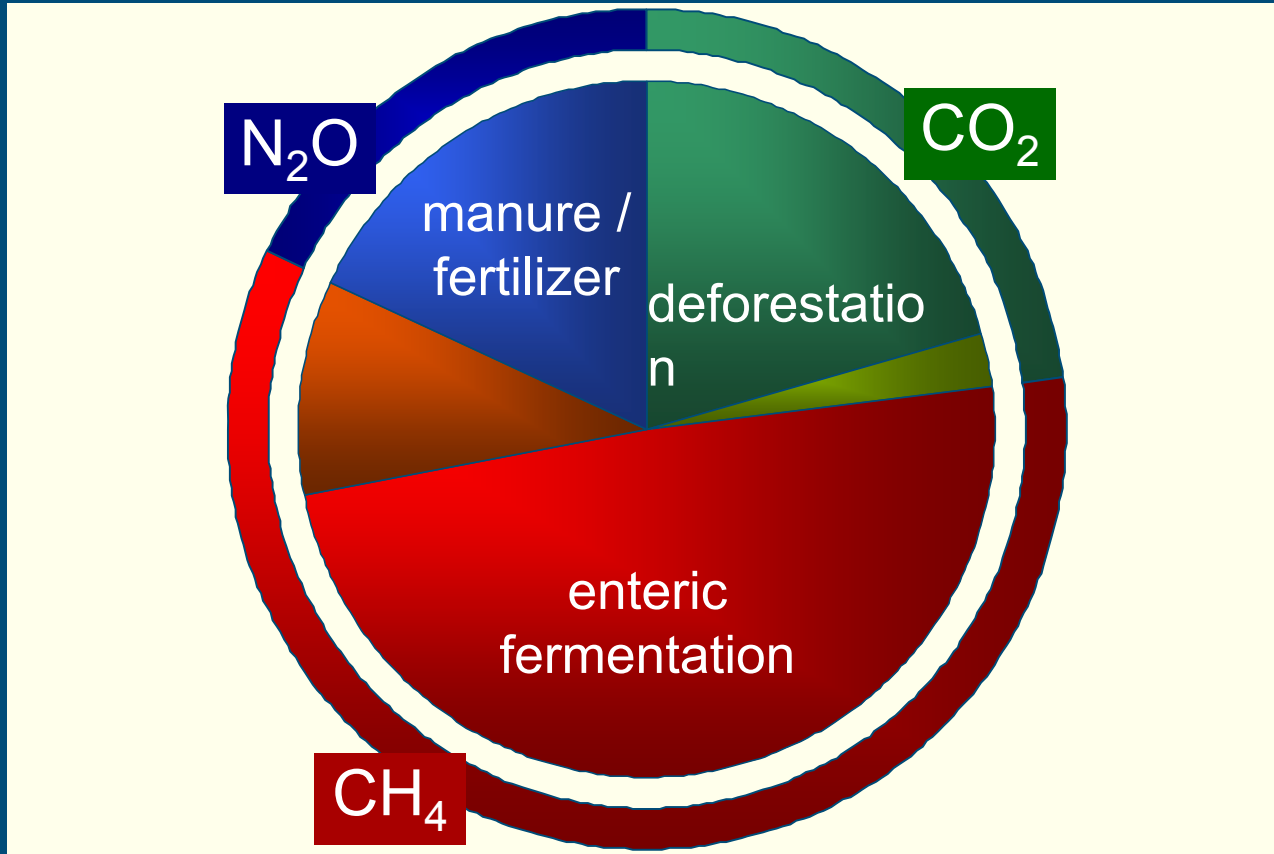
*Global Warming Potential





Livestock greenhouse gases

FAO (2006)



GWP* -20 yr:

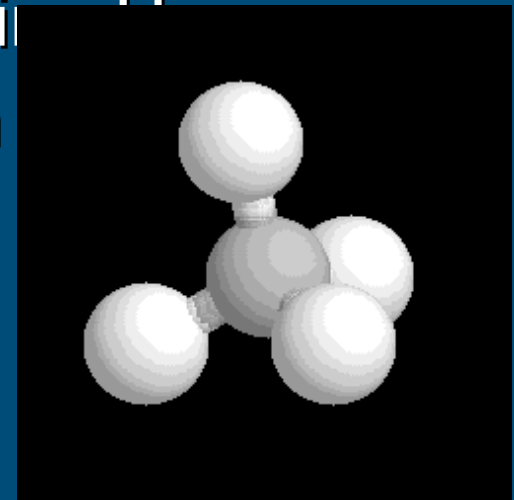
CO ₂	1
CH ₄	72
N ₂ O	289

*Global Warming Potential

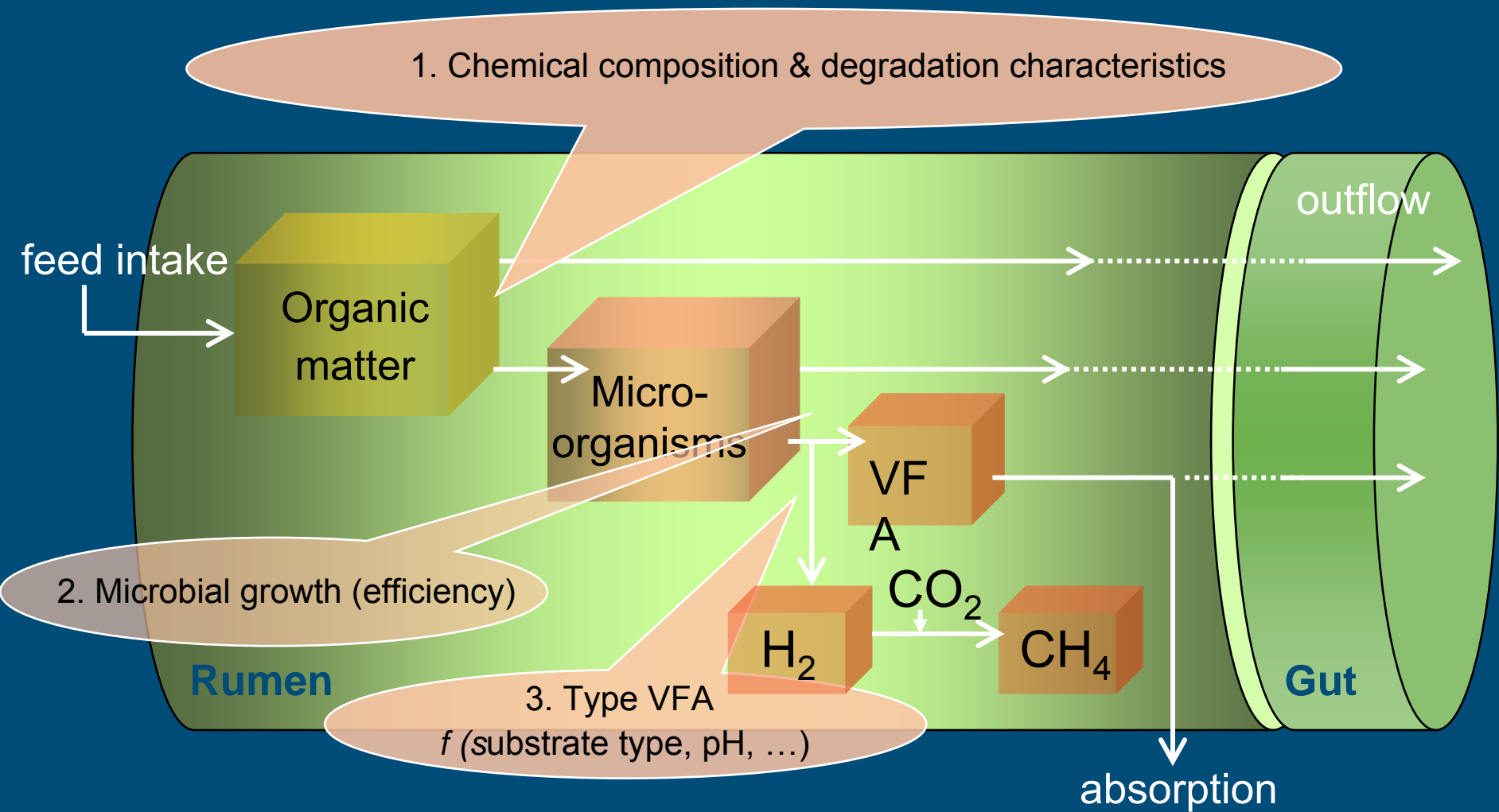


Rumen methanogenesis

- Fermentative micro-organisms utilize dietary organic matter to produce VFA plus gases (e.g., CO_2 , H_2)
 - amount of H_2 depends on type of VFA
- Methanogens reduce CO_2 to CH_4 using H_2 , keeping H_2 partial pressure in rumen low
- H_2 is used up as it is produced
- CH_4 production:
 - 2 – 12% of GE intake
 - 10 – 35 g/kg DM intake



Factors involved in rumen methanogenesis



Empirical models of methane production

- > 30 empirical models available
 - inventory
 - mitigation strategy
- Independent variables include live weight, milk production, feed intake, dietary components, digestibility
- Applied in models of greenhouse gas emissions in whole farm setting



Assessment of accuracy of empirical models

Ellis et al. (2010) *Global Change Biology*

- 9 methane equations applied in 8 whole farm models
- 169 observations from 9 studies

	Mean	SD	Min	Max
Feed intake (kg DM/d)	19.6	4.0	11.2	32.0
Milk production (kg/d)	30.3	9.05	8.8	49.4
Methane production (g/d)	371	77.1	117	698



Empirical models of methane production - 1

CH₄ production (g/d) estimated as:

- 274 (Europe) or 323 (N-America)

IPCC (1997) Tier I

- $0.06 \times \text{GE intake} / 55.65$

IPCC (1997) Tier II

- $137 + 10 \times \text{milk yield}$

Corre (2002)

- $10 + 4.9 \times \text{milk yield} + 1.5 \times \text{LW}^{0.75}$

Kirchgeßner et al. (1995) - 1



Empirical models of methane production - 2

CH₄ production (g/d) estimated as:

- $(45 - 0.02 \times \text{DMI}^2 - 1.8 \times \text{C18:2} - 84 \times \text{C} \geq 20) \times \text{DMI}$
- $[1.3 + 0.11 \times \text{Dig}_m + \text{Mn} \times (2.14 - 0.05 \times \text{inDig}_m)] \times 2003$
- $(3 + 0.5 \times \text{NSC} + 1.7 \times \text{HCBA} + 2.7 \times \text{CEP}) / 55.65$
Moe & Tyrrell (1979)
- $63 + 79 \times \text{CF} + 10 \times \text{NFE} + 26 \times \text{CP} - 212 \times \text{FAT}$
Kirchgeßner et al. (1995) - 2
- 20 x concentrate + 22 x maize sil + 27 x grass
(sil)



Evaluation of empirical methane models

Ellis et al. (2010)

	Pred CH ₄ (g/d)	
IPCC (1997) Tier I	304	
IPCC (1997) Tier II	399	
Corre (2002)	440	Observed CH ₄ 371 g/d
Kirchgeßner et al. (1995) – 1	404	
Giger-Reverdin et al. (2003)	230	
Blaxter & Clapperton (1965)	332	
Moe & Tyrrell (1979)	391	
Kirchgeßner et al. (1995) – 2	345	
Schils et al. (2006)	483	



Evaluation of empirical methane models

Ellis et al. (2010)

	Pred CH ₄ (g/d)	RMSPE (%)
IPCC (1997) Tier I	304	27.6
IPCC (1997) Tier II	399	20.9
Corre (2002)	440	34.2
Kirchgeßner et al. (1995) – 1	404	29.5
Giger-Reverdin et al. (2003)	230	52.5
Blaxter & Clapperton (1965)	332	21.2
Moe & Tyrrell (1979)	391	20.2
Kirchgeßner et al. (1995) – 2	345	20.9
Schils et al. (2006)	483	39.5



Evaluation of empirical methane models

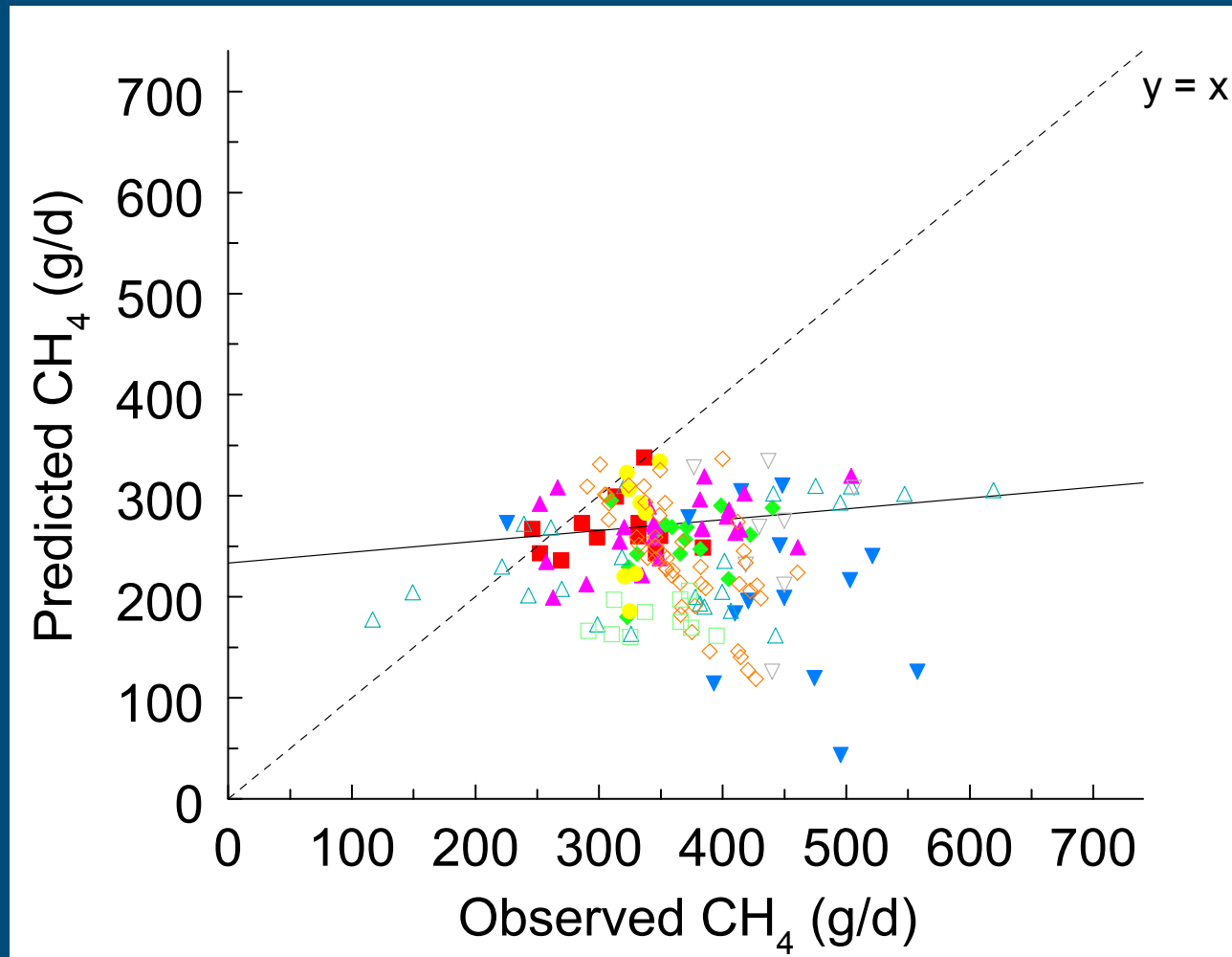
Ellis et al. (2010)

	Pred CH ₄ (g/d)	RMSPE (%)	CCC
IPCC (1997) Tier I	304	27.6	0.01
IPCC (1997) Tier II	399	20.9	0.49
Corre (2002)	440	34.2	0.13
Kirchgeßner et al. (1995) – 1	404	29.5	0.29
Giger-Reverdin et al. (2003)	230	52.5	0.12
Blaxter & Clapperton (1965)	332	21.2	0.27
Moe & Tyrrell (1979)	391	20.2	0.46
Kirchgeßner et al. (1995) – 2	345	20.9	0.22
Schils et al. (2006)	483	39.5	0.25



Evaluation of empirical methane models

Ellis et al. (2010)

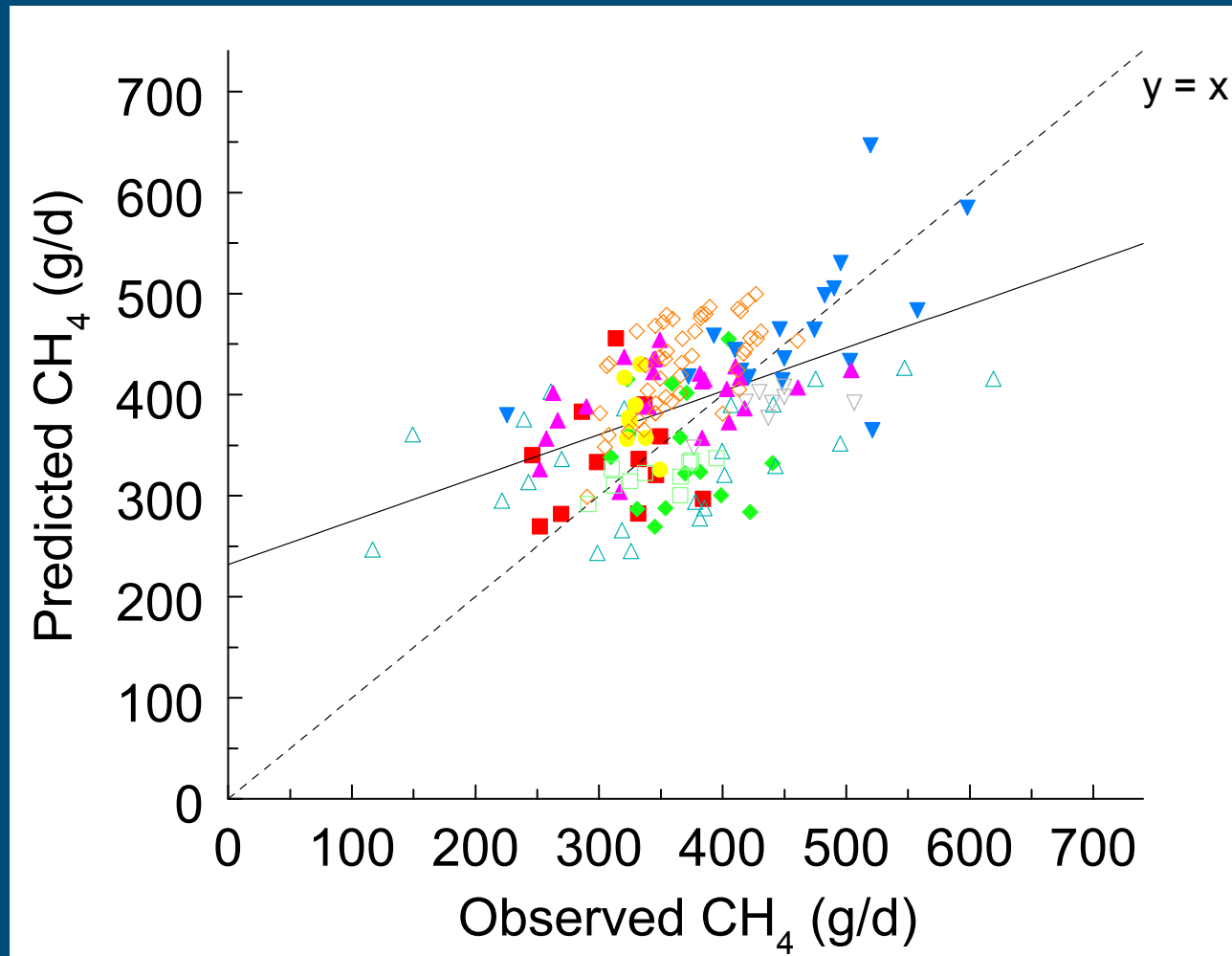


Model:
Giger-Reverdin
et al. (2003)



Evaluation of empirical methane models

Ellis et al. (2010)



Model:

Moe & Tyrrell
(1979)



Conclusions empirical methane models

- Simple, generalized models performed worse than models based on diet composition
- Predictions poor; significant bias and deviation of regression slope from unity
- Substantial errors into inventories of whole farm greenhouse gas emissions are likely
- Low prediction error may lead to incorrect mitigation recommendations



Overview

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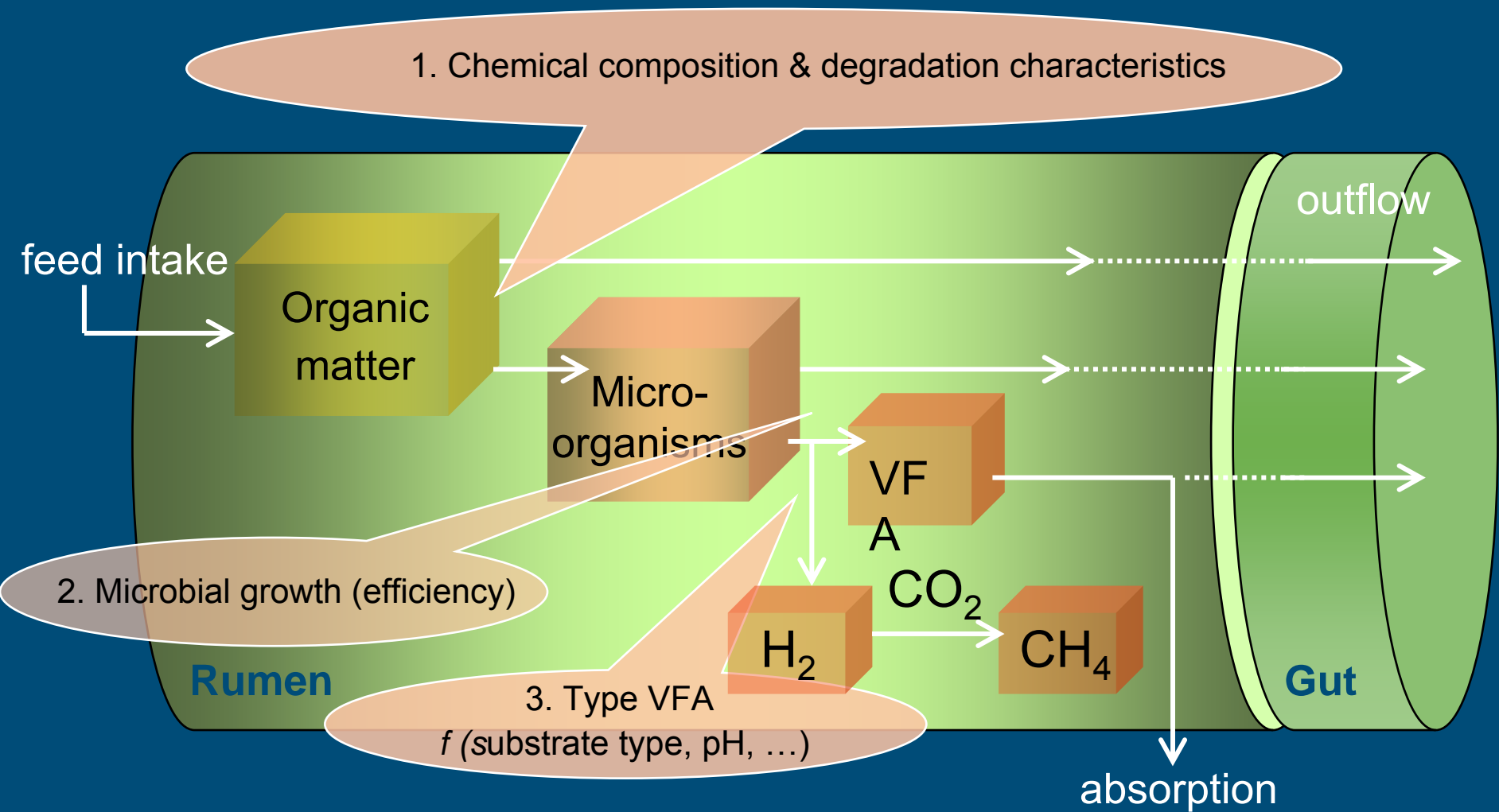


Rate : state formalism

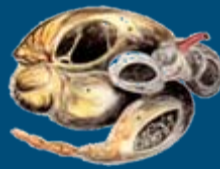
- State variables: Q_1, Q_2, \dots, Q_n
- Change of state variables with time t
 - $dQ_1/dt = f_1(Q_1, Q_2, \dots, Q_n; P)$
 - $dQ_2/dt = f_2(Q_1, Q_2, \dots, Q_n; P)$
 - \vdots
 - \vdots
 - $dQ_n/dt = f_n(Q_1, Q_2, \dots, Q_n; P)$
- Differential equations based on law of mass conservation, 1st law of thermodynamics, etc



Factors involved in rumen methanogenesis



Mechanistic rumen module



Dijkstra et al. (1992)

Modifications:

Dijkstra (1994)

Mills et al. (2001)

Dijkstra et al. (2002)

Kebreab et al. (2004)

Bannink et al. (2006)

In use in:

Netherlands

UK

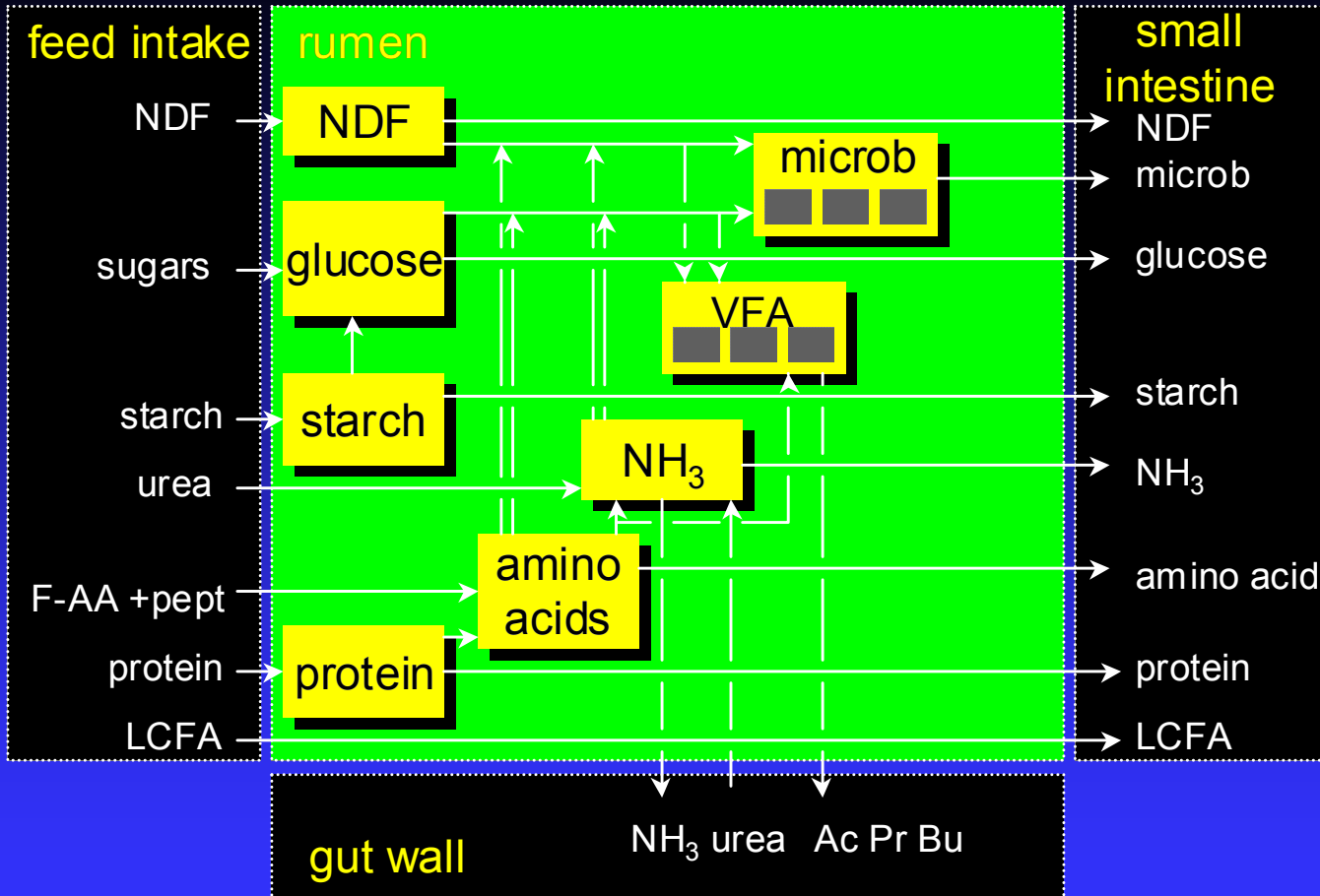
Australia

Brazil

Canada

USA

and many more



J. Dijkstra

Modelling methane emissions

Efficiency of microbial growth

- Substrate is used for
 - ✓ non-growth purposes ('maintenance')
 - ✓ growth purposes

- Yield is related to fractional growth rate (Pirt, 1965)

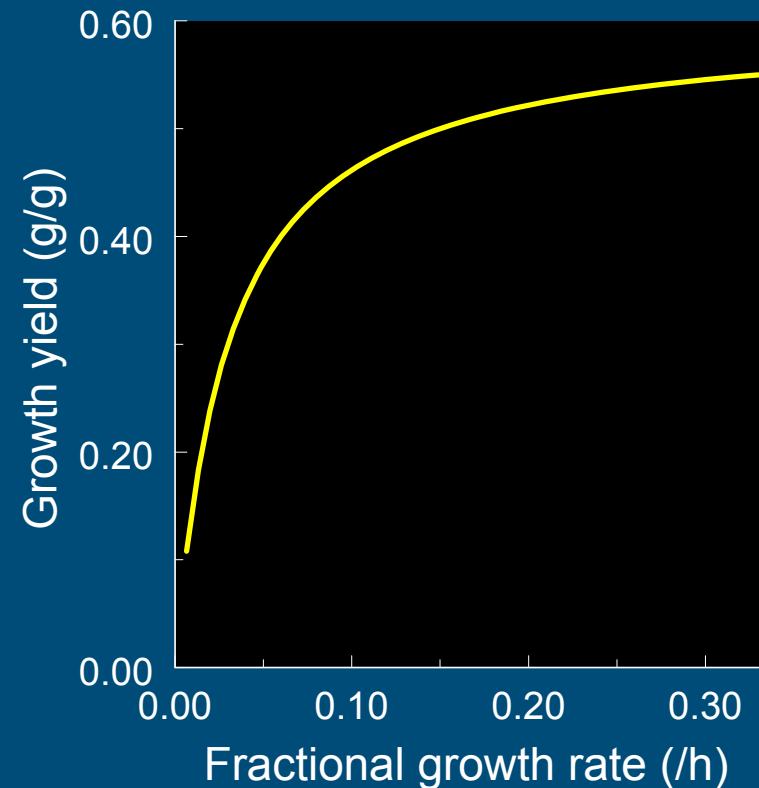
$$1 / Y = M / \mu + 1 / Y_{\max}$$

Y = growth yield

M = maintenance requirement

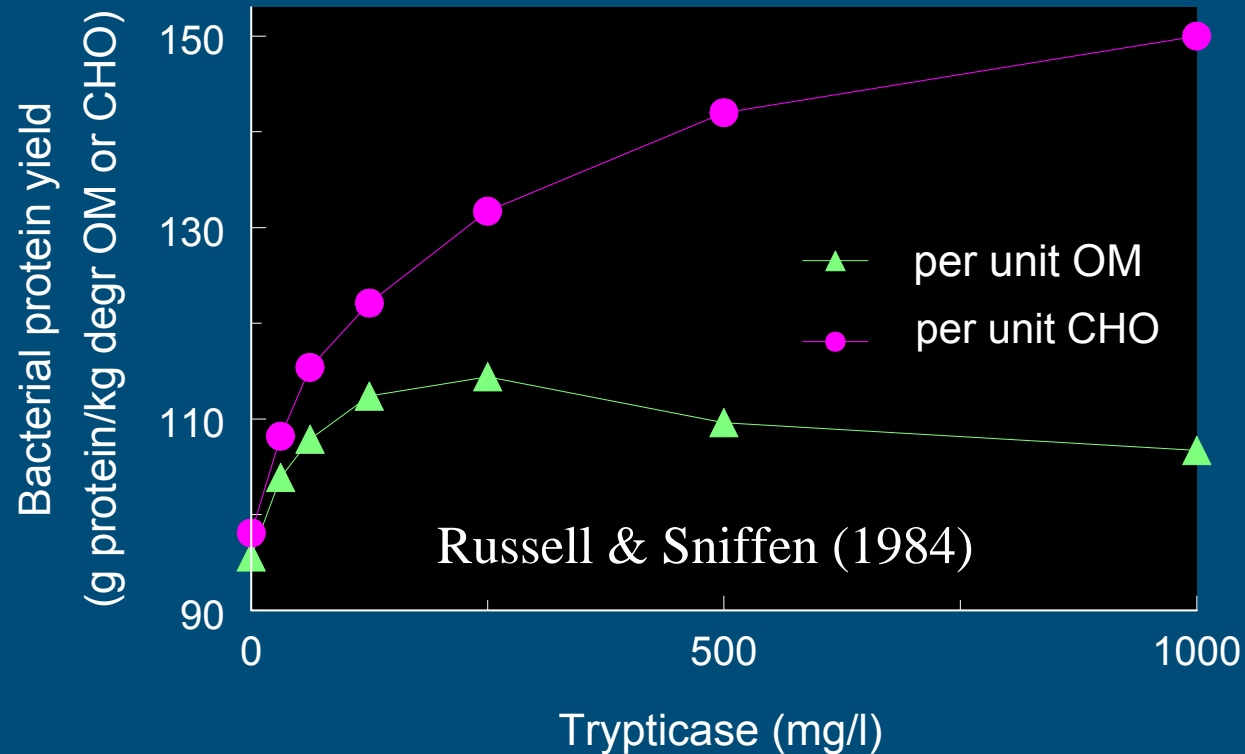
Y_{\max} = maximum yield

μ = fractional growth rate



Microbial metabolism: N source

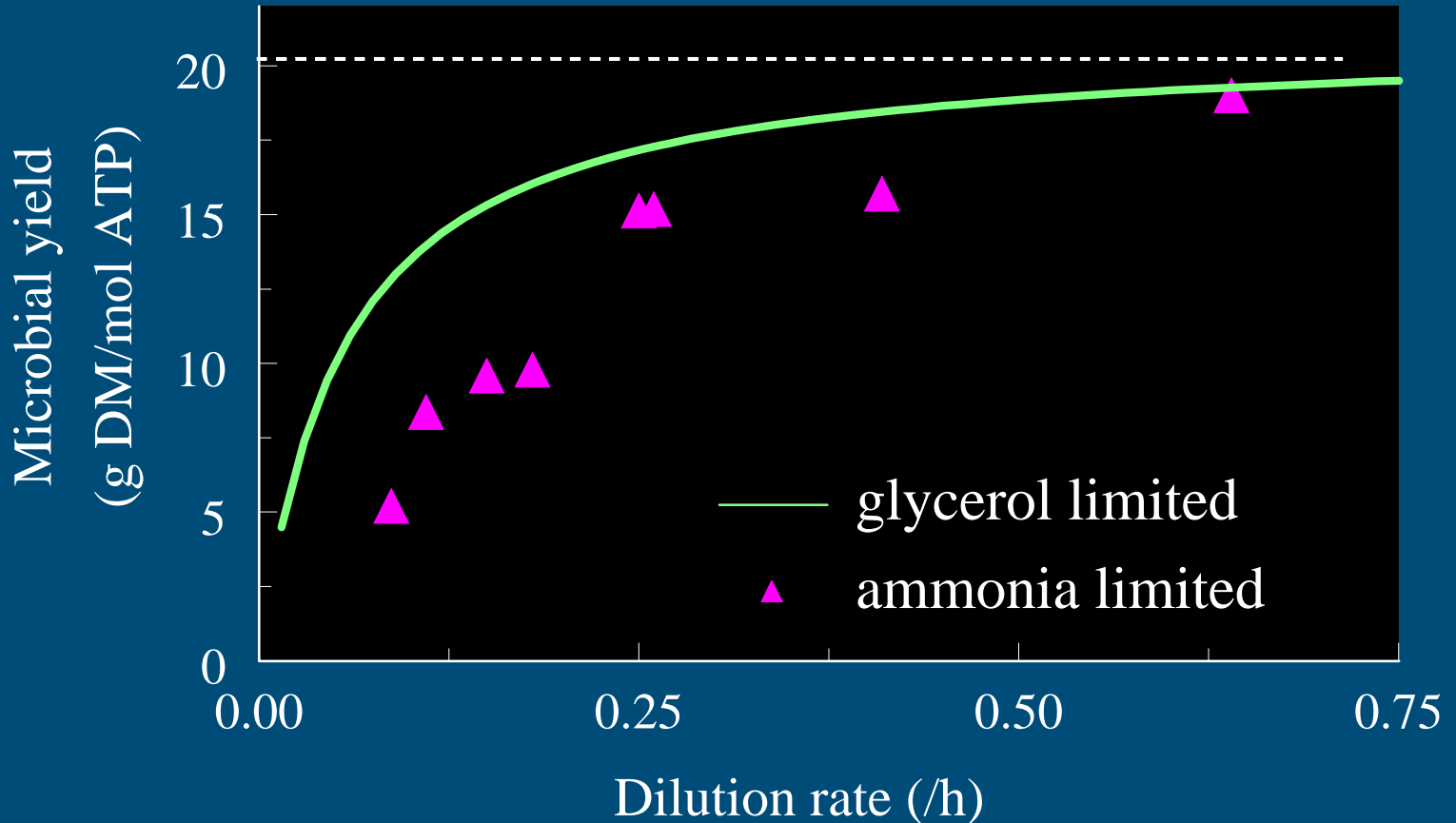
Yield affected by availability of preformed molecules



Energy and N synchrony: energy spilling

K. aerogenes; Neijssel & Tempest (1976)

$$U_{\text{glycerol in energy spilling}} = v_{\text{max}} Q_{\text{microbes}} / (1 + [\text{ammonia}] / J_{\text{ammonia}})$$



Significance of VFA molar proportion

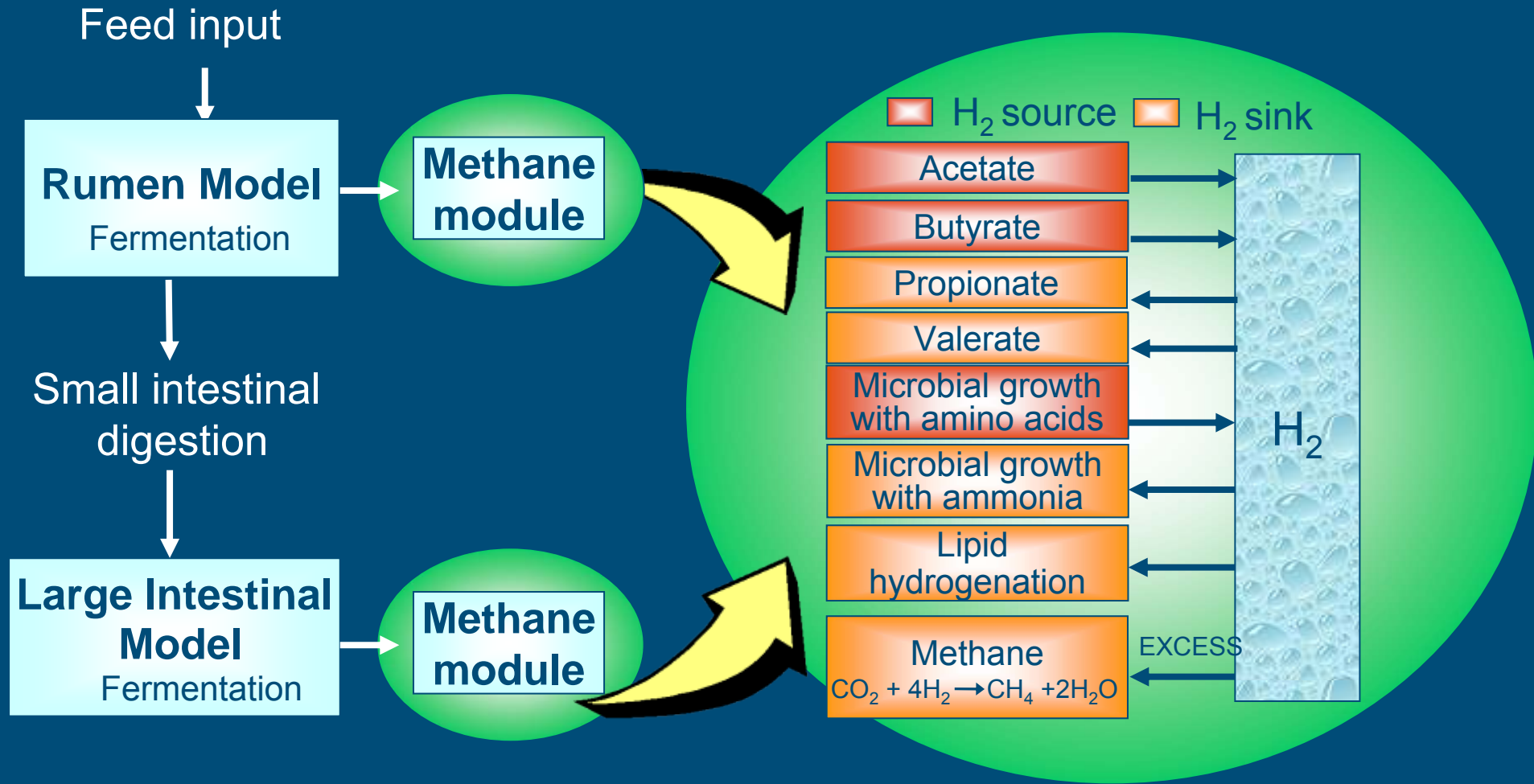


acetate	70%	60%
propionate	15%	25%
butyrate	15%	15%
CH ₄	0.39 mol/mol VFA	0.31 mol/mol VFA



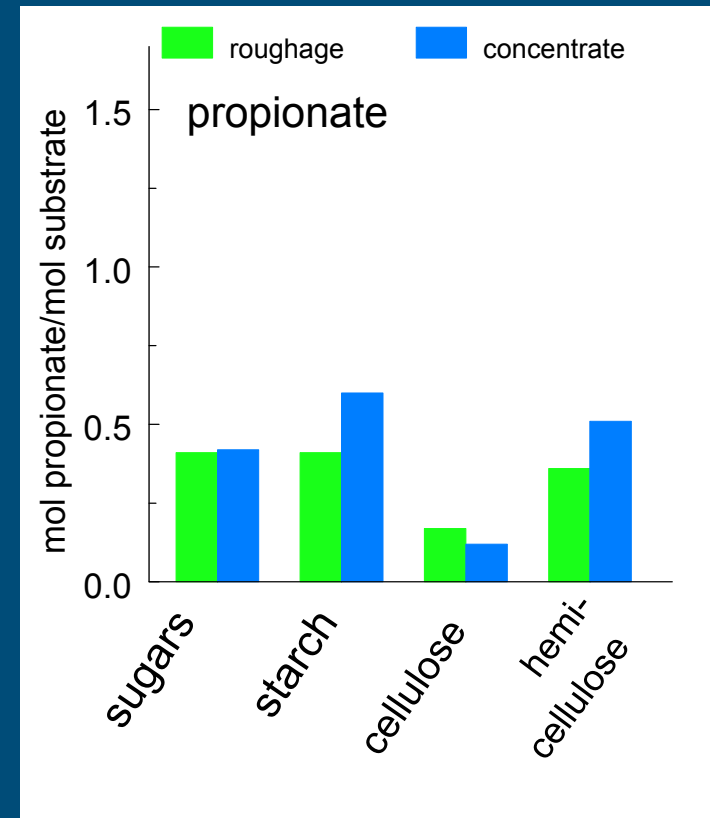
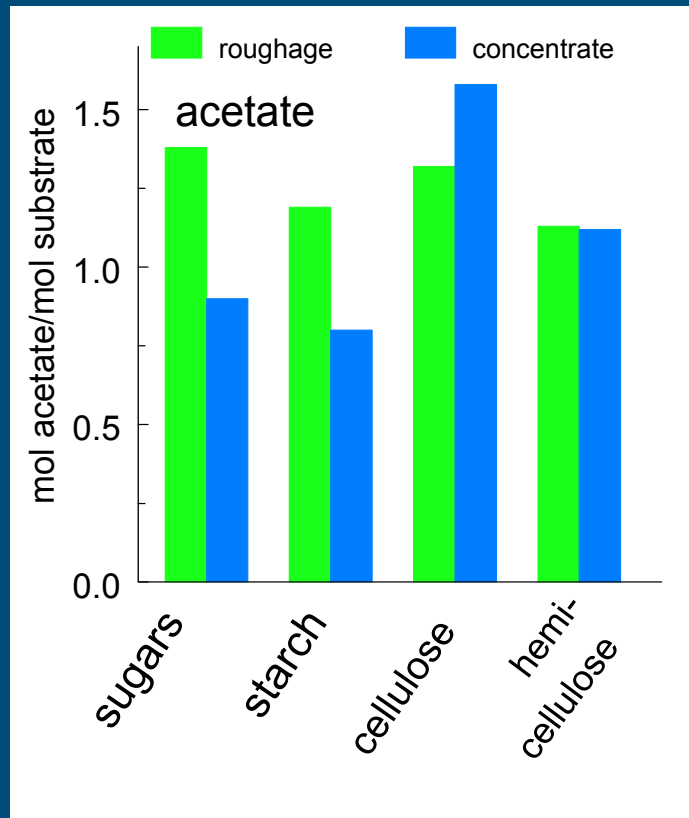
Mechanistic model methane production

(Dijkstra et al. 1992; Mills et al. 2001; Bannink et al. 2006)



VFA stoichiometry

- Type of VFA formed related to substrate fermented, rumen pH, roughage vs concentrate

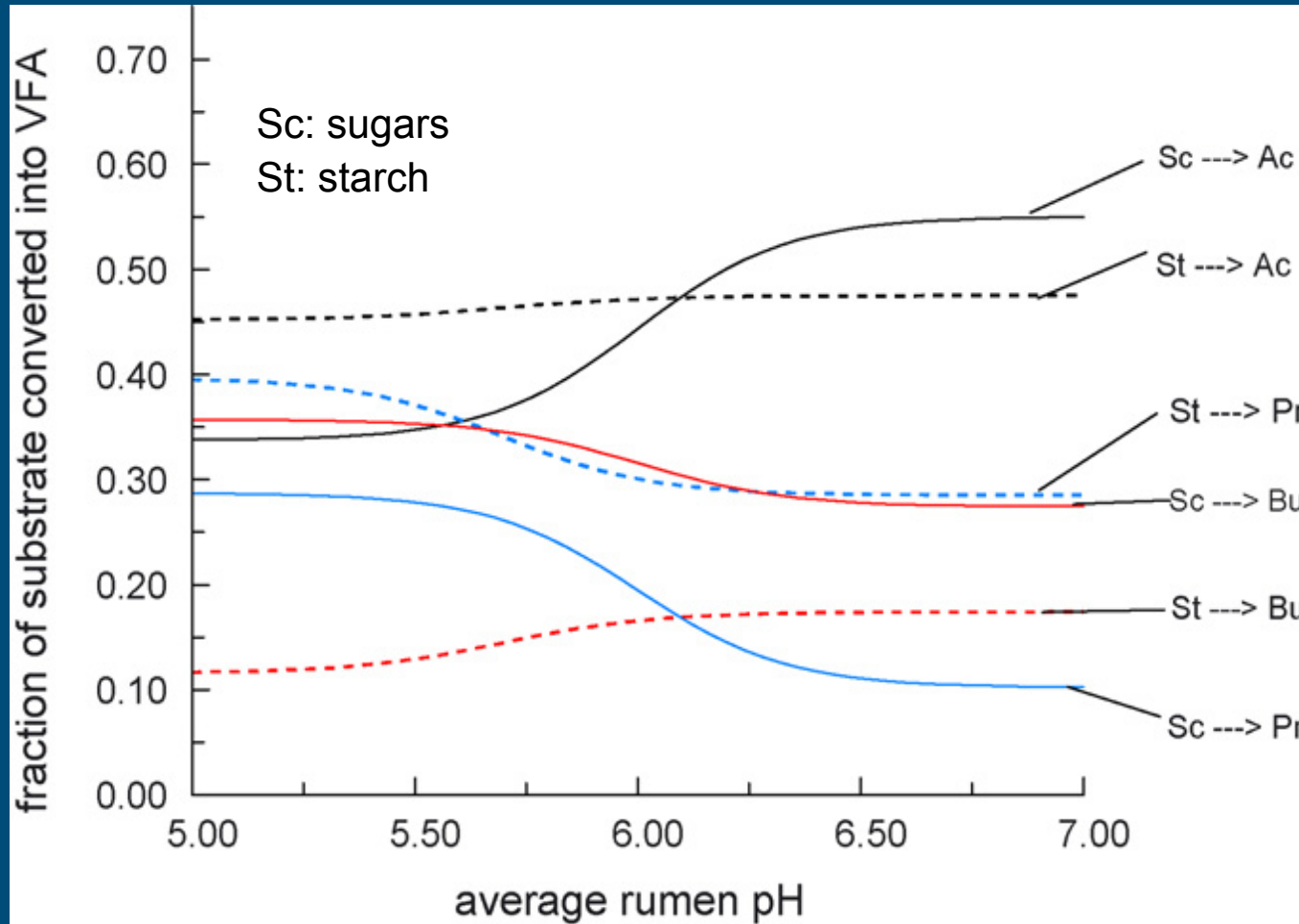


Murphy et al.
(1984)



VFA stoichiometry and rumen pH

Bannink et al. (2008)



In vivo data

rumen
digestion
lactating cows

Analysis

substrate type

roughage vs.
concentrates

efficiency

microbial
growth

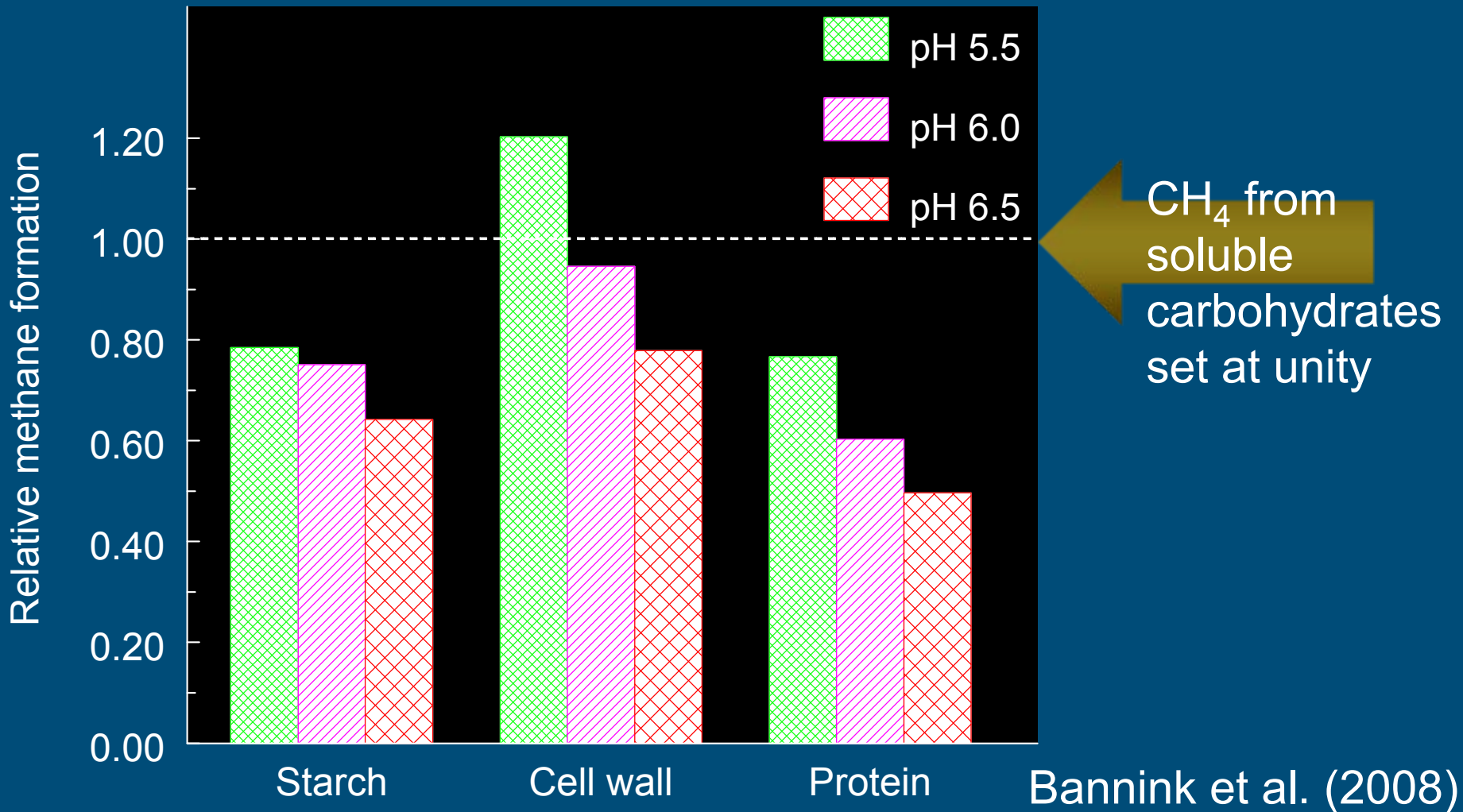
kinetics

VFA-absorption

pH



Methane formation from various substrates



Mechanistic models of methane formation

- Prediction based on description of the rumen in terms of components and associated processes
- Mechanistic models superior predictive power
Benchaar et al. (1998); Mills et al. (2001); Kebreab et al. (2006)
- Allows evaluation of dietary mitigation options
 - Inventories under Kyoto protocol

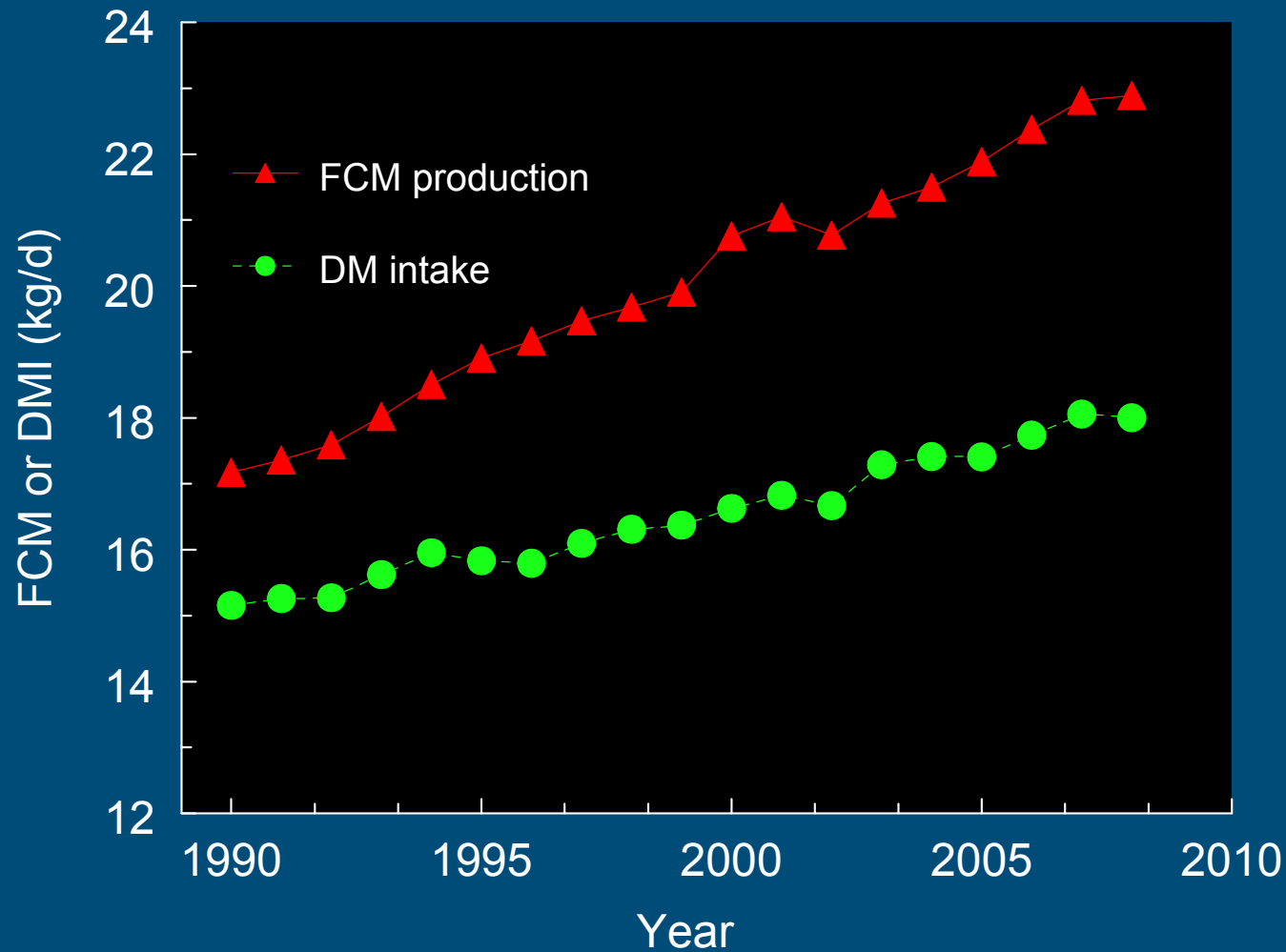


Example: Netherlands, database 1990 - 2008

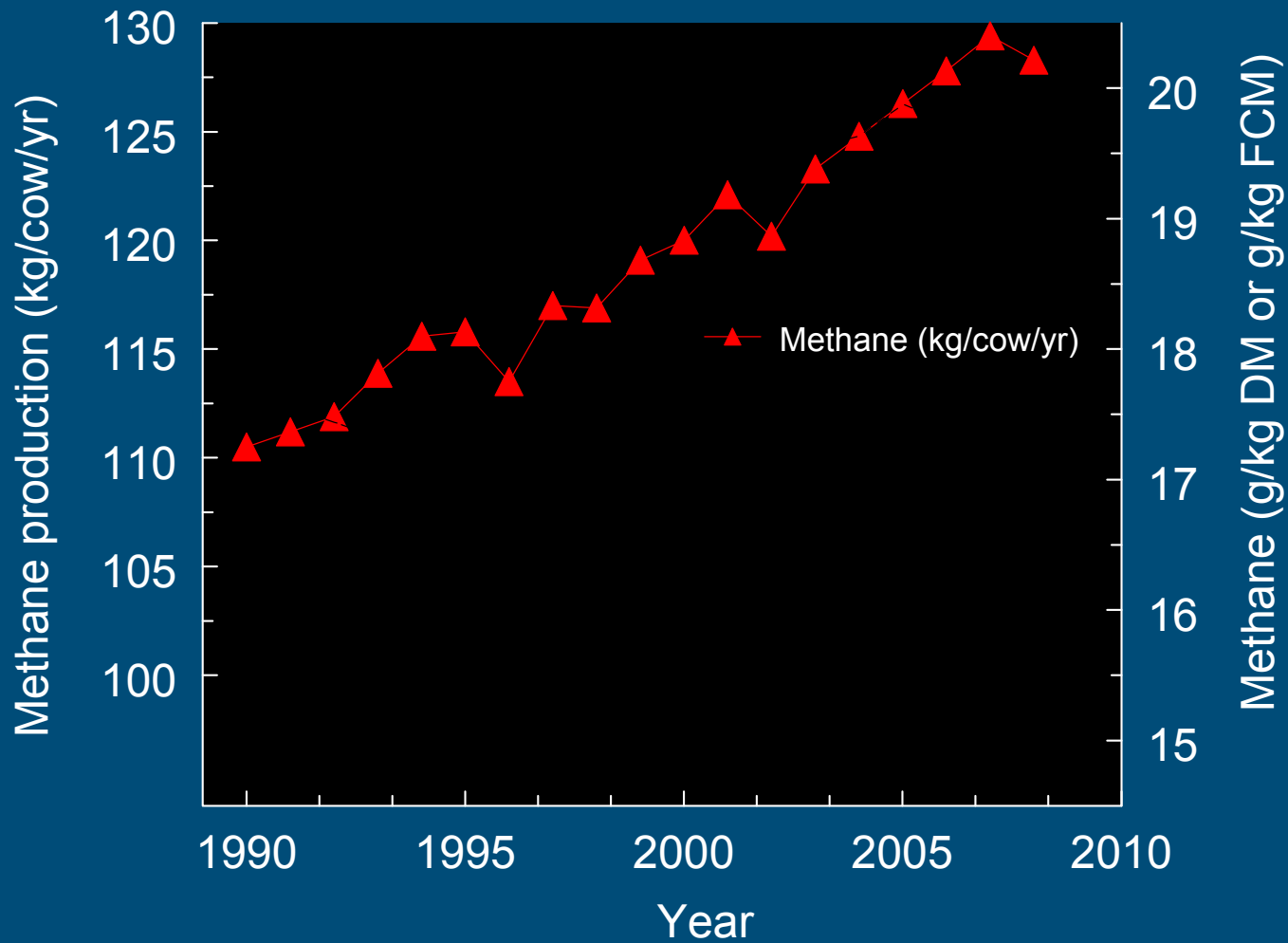
- Milk production and composition data
- Feed intake data
 - feed categories: fresh grass, grass silage, maize silage, wet byproducts, concentrates
 - concentrate chemical composition from central database
 - roughage chemical composition from Laboratory for Soil and Crop Testing
- Dietary changes in 1990 – 2008
 - more maize silage and less fresh grass
 - crude protein content decreased



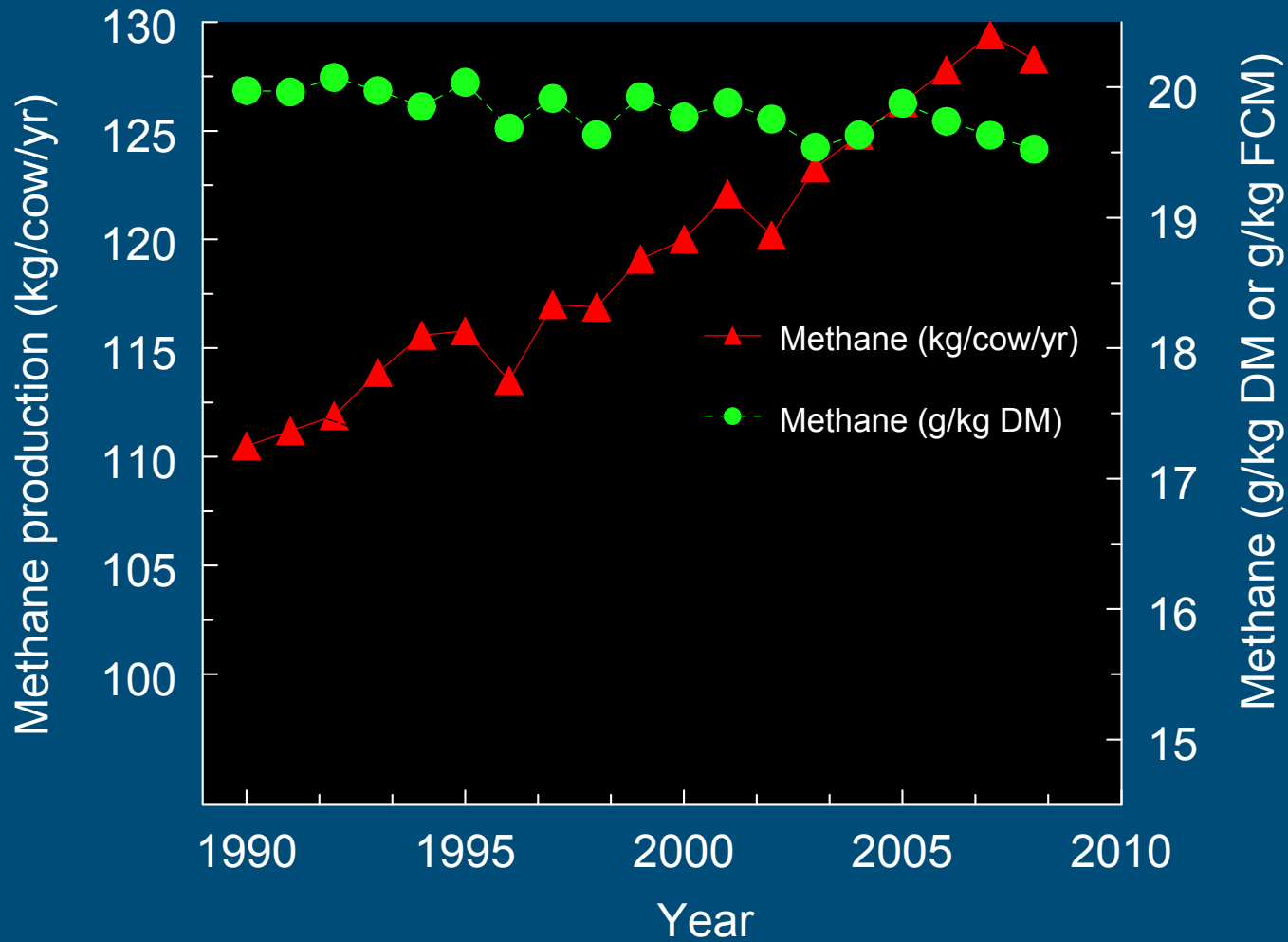
DM intake and fat corrected milk (FCM)



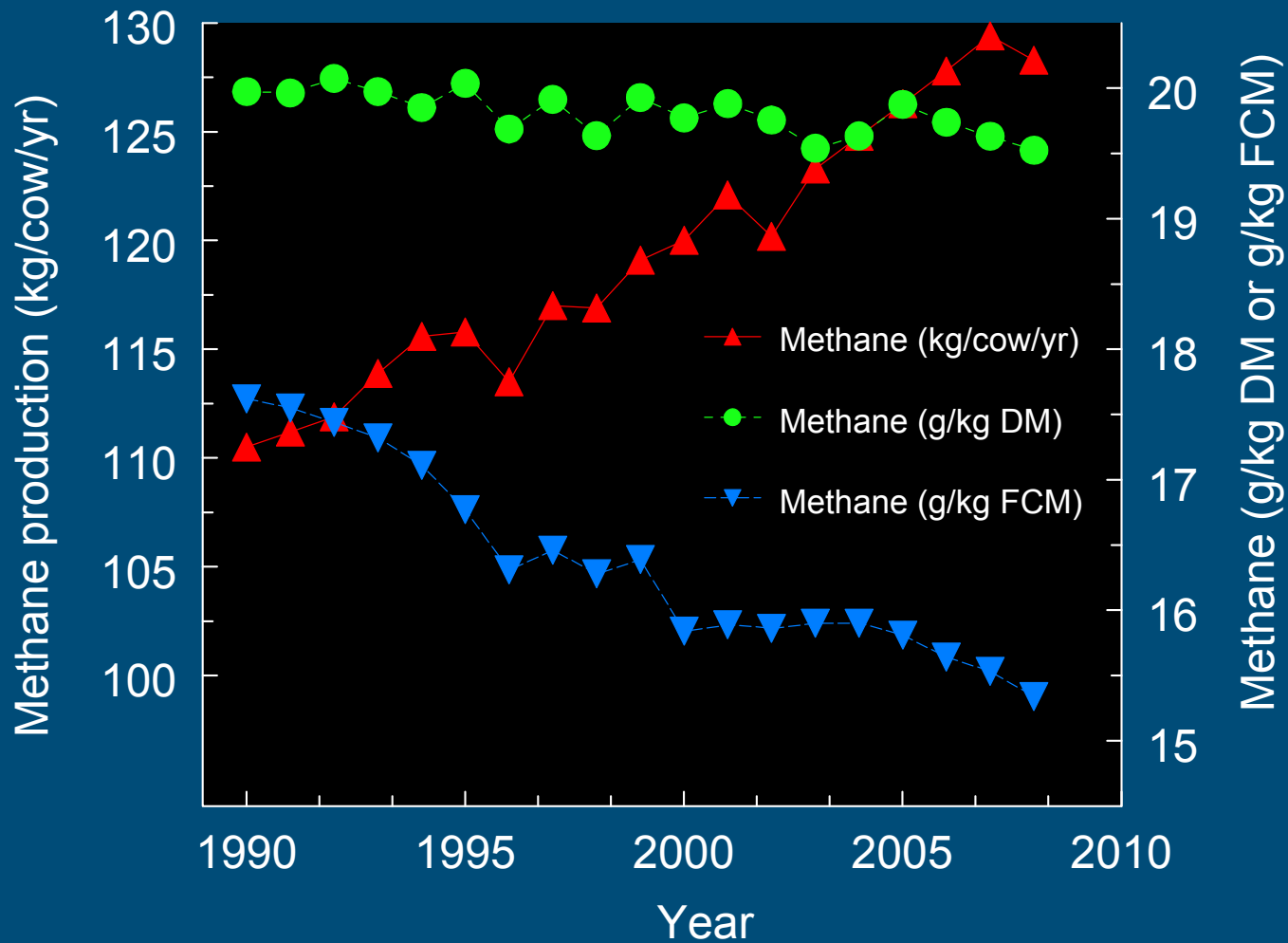
Simulated methane production



Simulated methane production



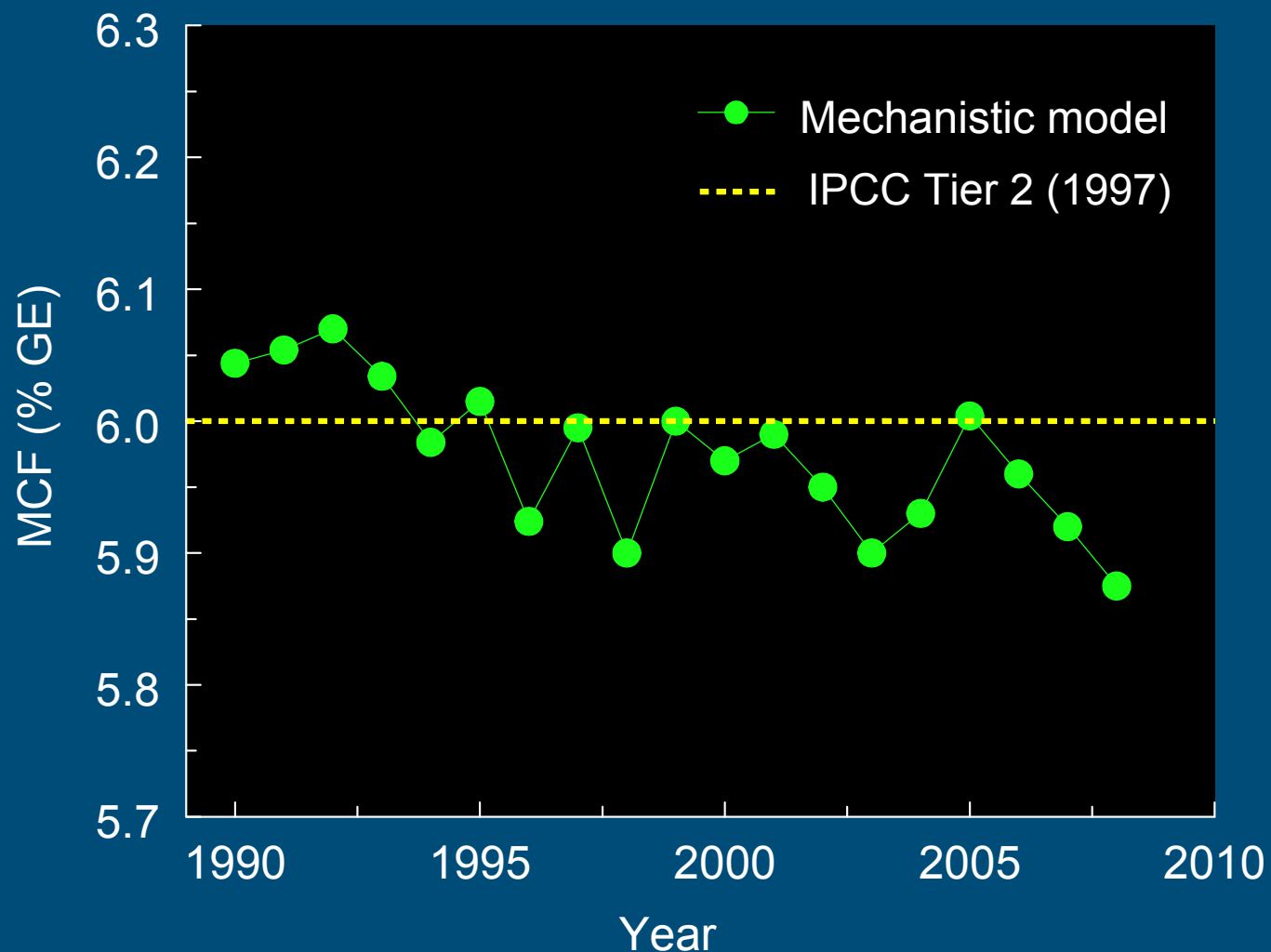
Simulated methane production



Methane Conversion Factor (MCF)

Trend methane production (kg/cow/yr):

IPCC 1.38
model 1.05



Conclusions mechanistic methane models

- Mechanistic methane models enable prediction based on understanding of the system
- Continued interaction between mechanistic modelling and experimentation allows faster progress
 - combine expertise in traditional fermentation parameters, molecular microbiological tools, and mathematics



Acknowledgements

- Andre Bannink – Lelystad, the Netherlands
- Jennifer Ellis – Univ Guelph, Canada
- James France – Univ Guelph, Canada
- Ermias Kebreab – Univ Davis, USA
- Secundino Lopez – Univ Leon, Spain

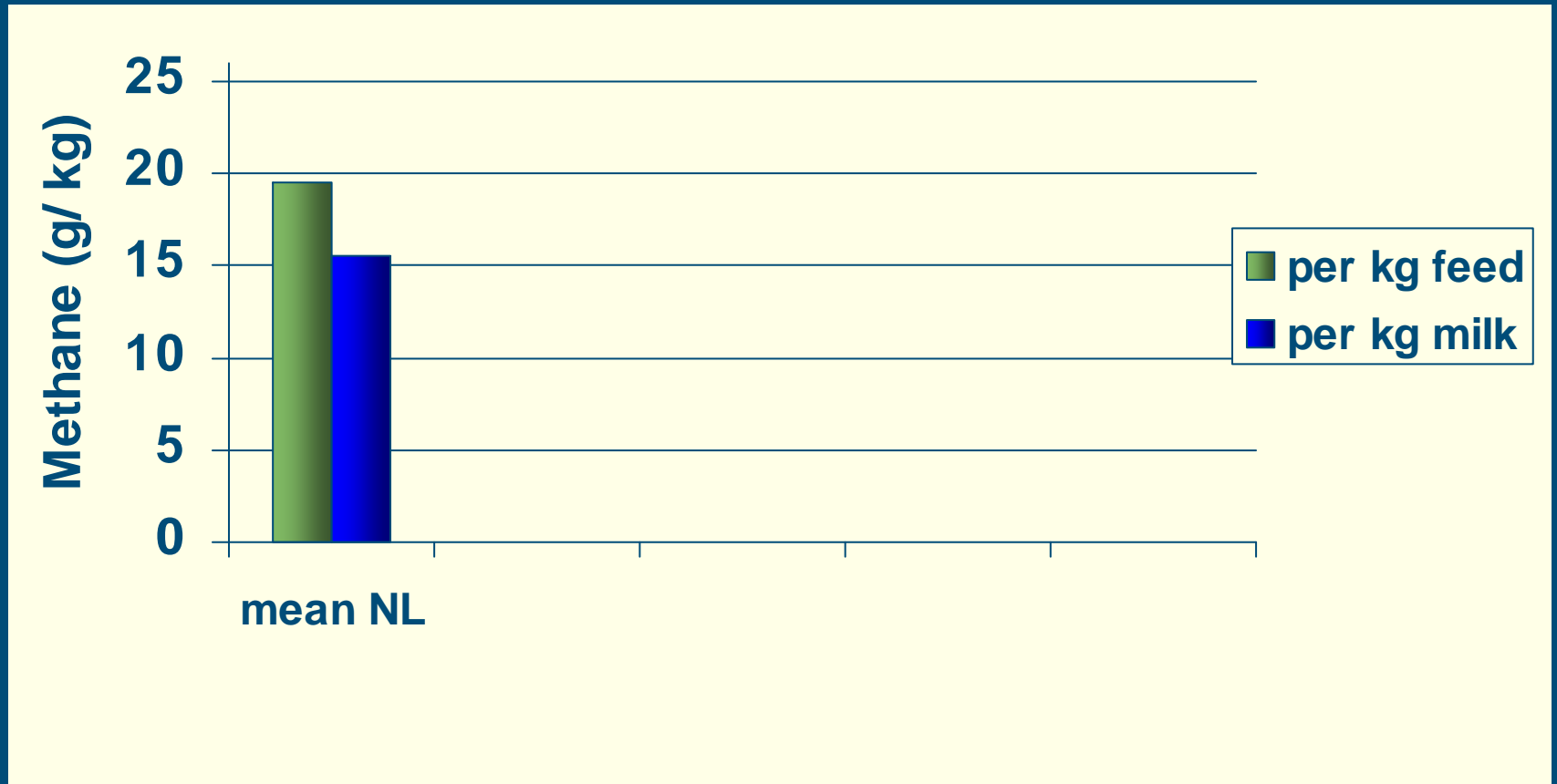


Acknowledgements

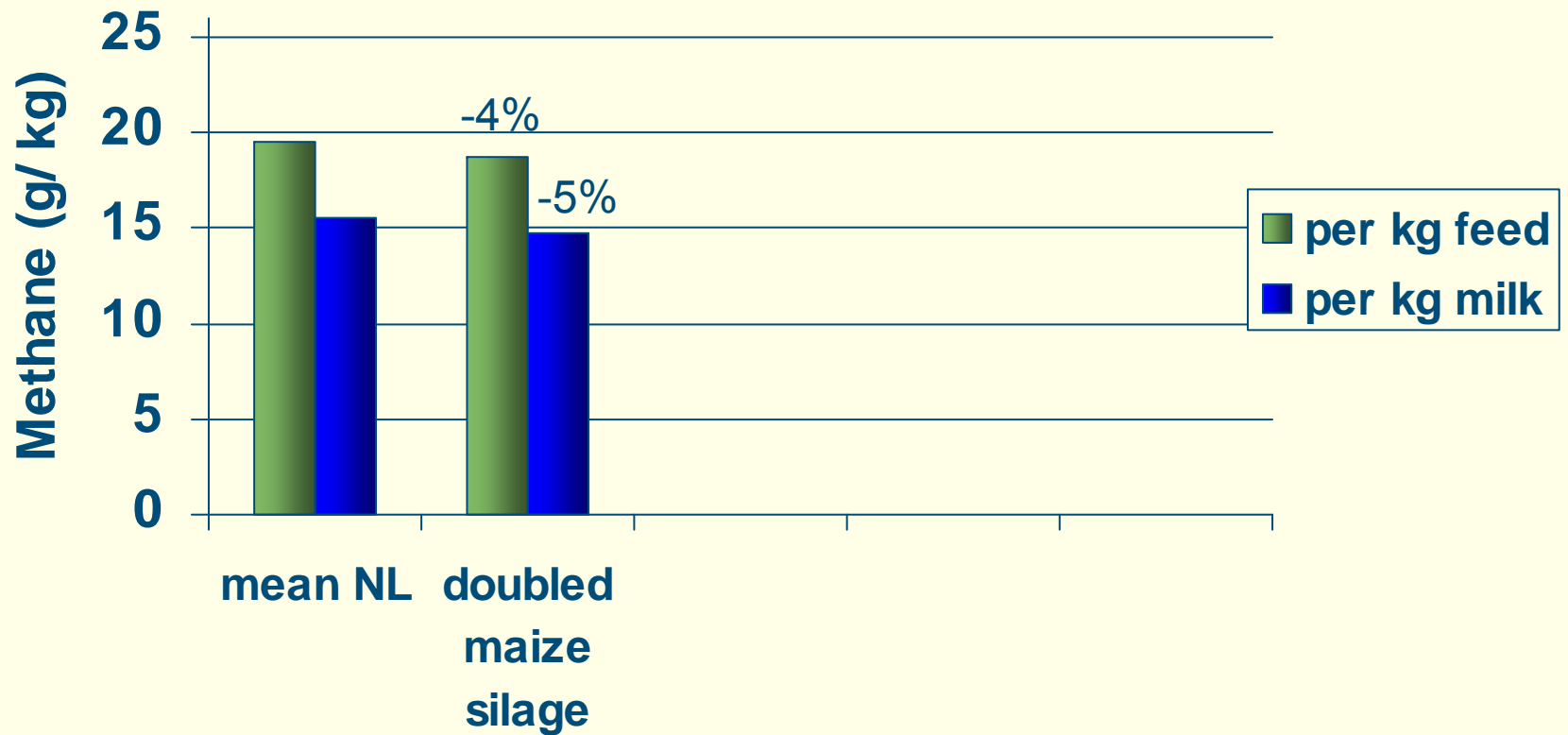
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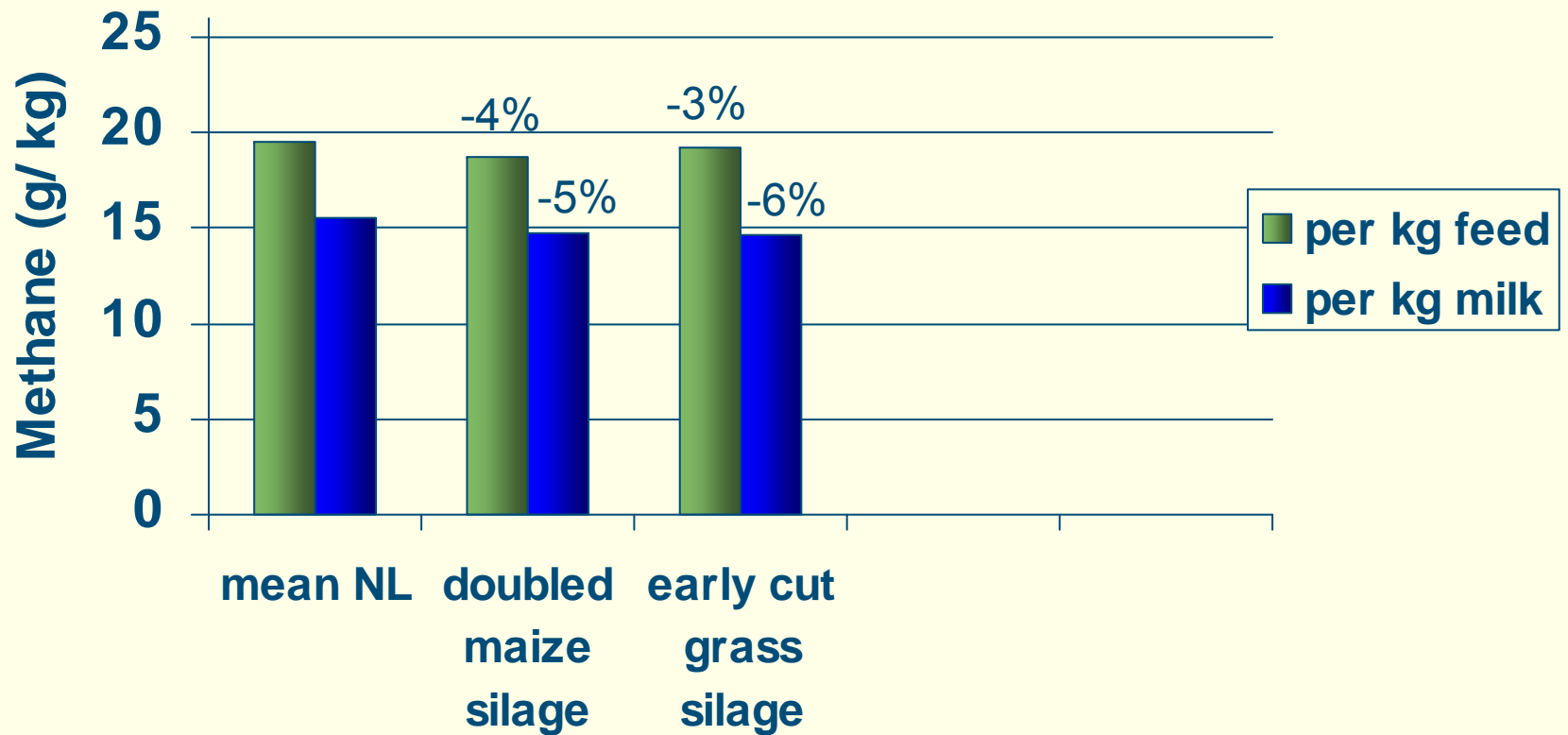
Practical solutions: model results



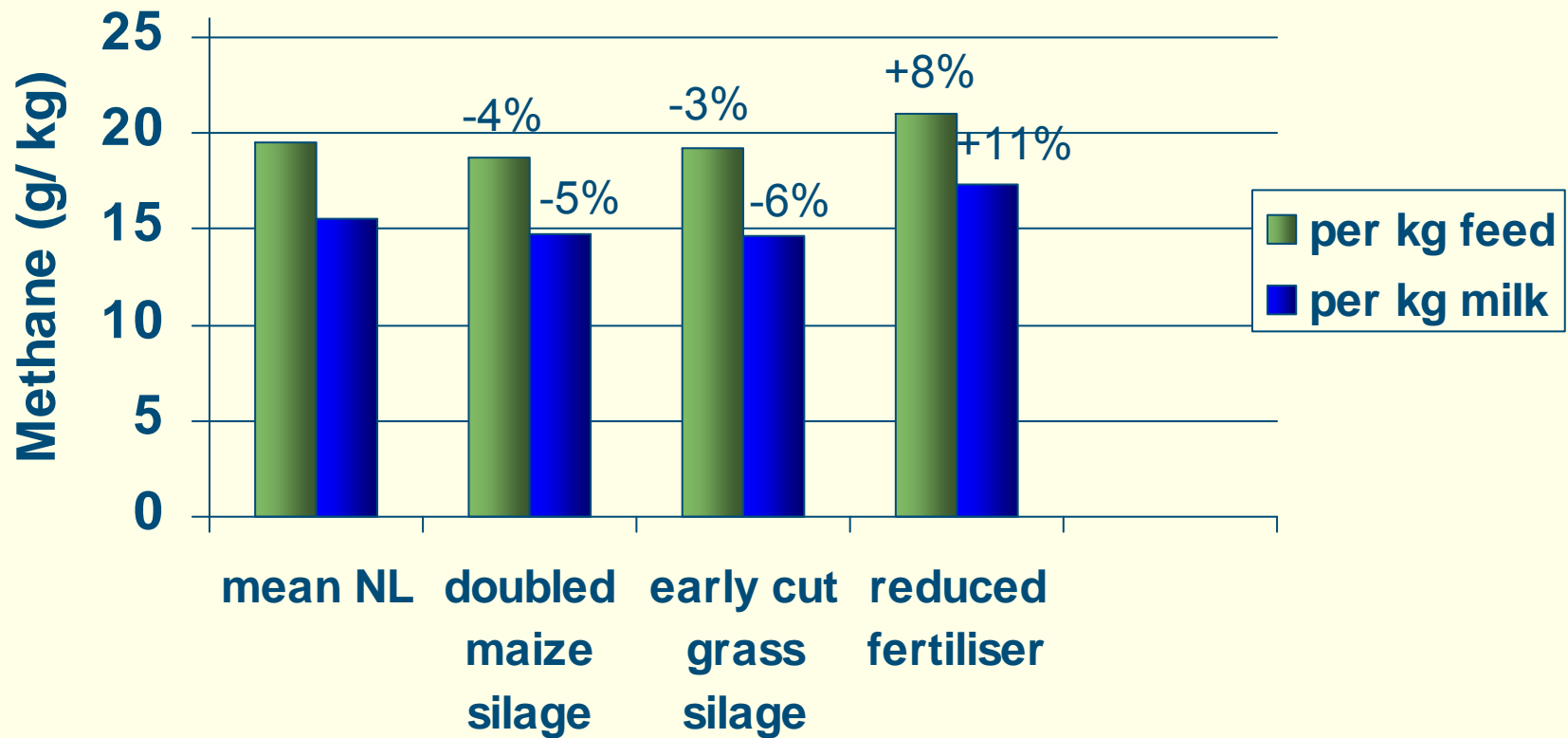
Practical solutions: model results



Practical solutions: model results



Practical solutions: model results



Practical solutions: model results

